

- Interest points detectors
- Descriptors

- **Interest points detectors**
- Descriptors

From the talk:
Matching with Invariant Features

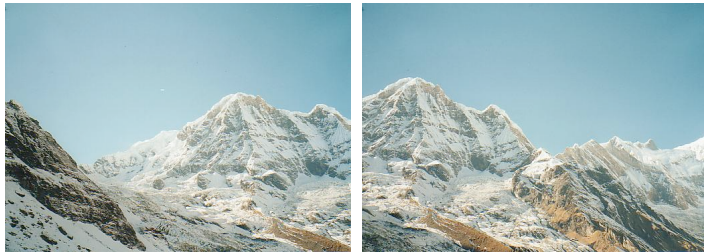
Darya Frolova, Denis Simakov
The Weizmann Institute of Science
March 2004

Example: Build a Panorama



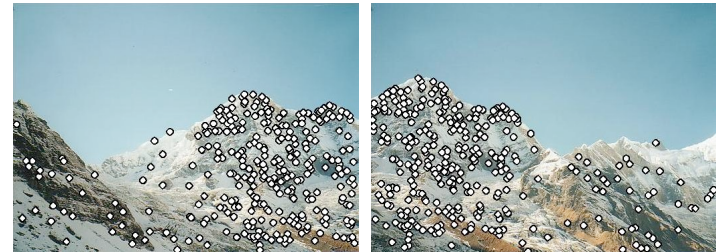
How do we build panorama?

- We need to match (align) images



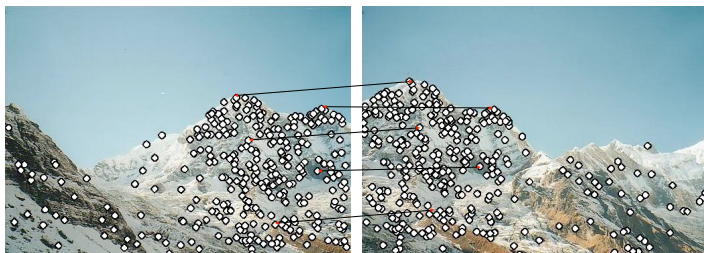
Matching with Features

- Detect feature points in both images



Matching with Features

- Detect feature points in both images
- Find corresponding pairs



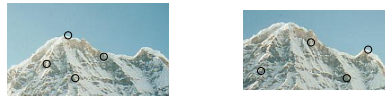
Matching with Features

- Detect feature points in both images
- Find corresponding pairs
- Use these pairs to align images



Matching with Features

- Problem 1:
 - Detect the *same* point *independently* in both images



no chance to match!

We need a repeatable detector

Matching with Features

- Problem 2:
 - For each point correctly recognize the corresponding one



We need a reliable and distinctive descriptor

More motivation...

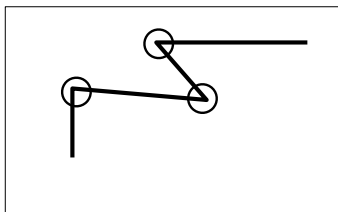
- Feature points are used also for:
 - Image alignment (homography, fundamental matrix)
 - 3D reconstruction
 - Motion tracking
 - Object recognition
 - Indexing and database retrieval
 - Robot navigation
 - ... other

Contents

- Harris Corner Detector
 - Description
 - Analysis
- Detectors
 - Rotation invariant
 - Scale invariant
 - Affine invariant
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 - Scale invariant
 - Affine invariant

An introductory example:

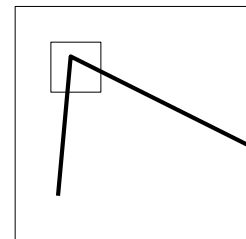
Harris corner detector



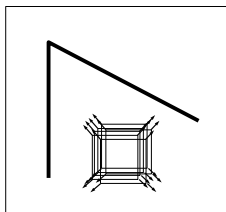
C.Harris, M.Stephens. "A Combined Corner and Edge Detector". 1988

The Basic Idea

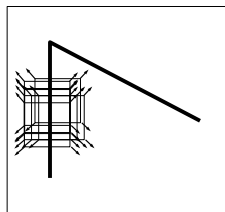
- We should easily recognize the point by looking through a small window
- Shifting a window in *any direction* should give a *large change* in intensity



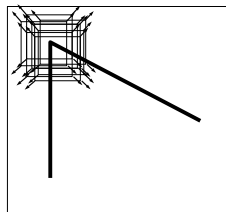
Harris Detector: Basic Idea



“flat” region:
no change in
all directions



“edge”:
no change along
the edge direction



“corner”:
significant change
in all directions

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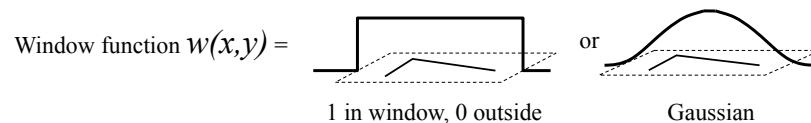
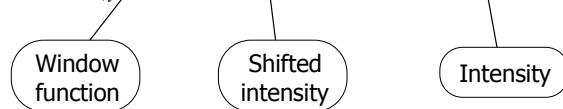
- Descriptors

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Harris Detector: Mathematics

Change of intensity for the shift $[u, v]$:

$$E(u, v) = \sum_{x, y} w(x, y) [I(x + u, y + v) - I(x, y)]^2$$



Harris Detector: Mathematics

For small shifts $[u, v]$ we have a *bilinear* approximation:

$$E(u, v) \approx [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

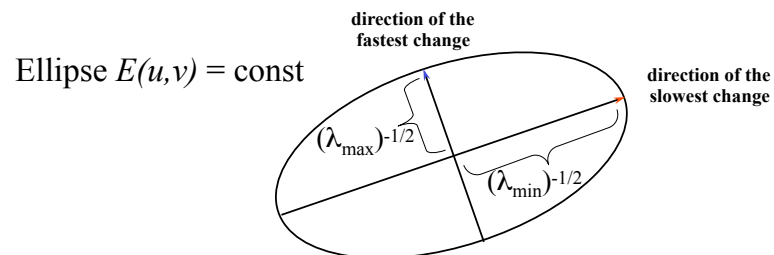
where M is a 2×2 matrix computed from image derivatives:

$$M = \sum_{x, y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Harris Detector: Mathematics

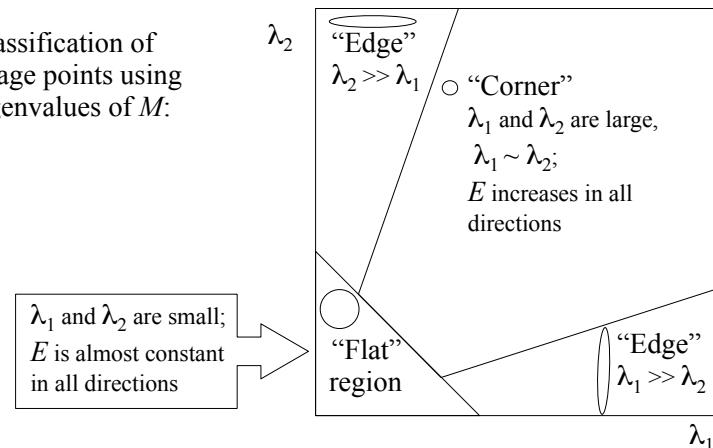
Intensity change in shifting window: eigenvalue analysis

$$E(u, v) \approx [u, v] M \begin{bmatrix} u \\ v \end{bmatrix} \quad \lambda_1, \lambda_2 - \text{eigenvalues of } M$$



Harris Detector: Mathematics

Classification of image points using eigenvalues of M :



Harris Detector: Mathematics

Measure of corner response:

$$R = \det M - k (\text{trace } M)^2$$

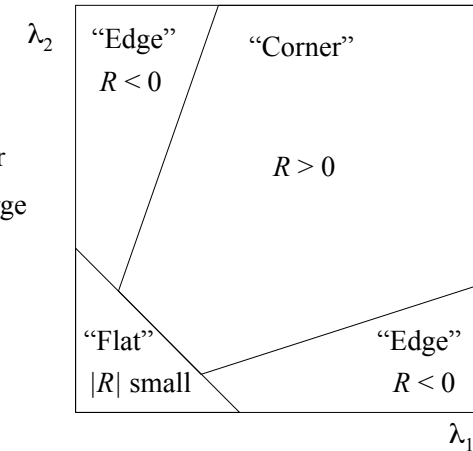
$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$

(k – empirical constant, $k = 0.04-0.06$)

Harris Detector: Mathematics

- R depends only on eigenvalues of M
- R is large for a corner
- R is negative with large magnitude for an edge
- $|R|$ is small for a flat region



Harris Detector

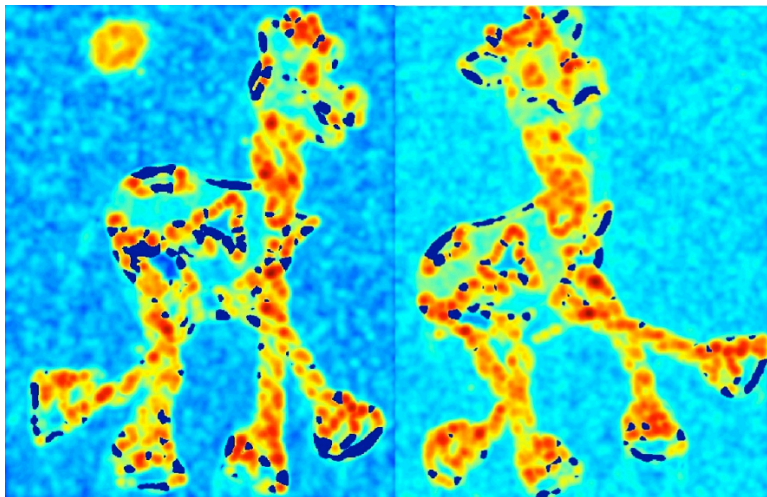
- The Algorithm:
 - Find points with large corner response function R ($R > \text{threshold}$)
 - Take the points of local maxima of R

Harris Detector: Workflow



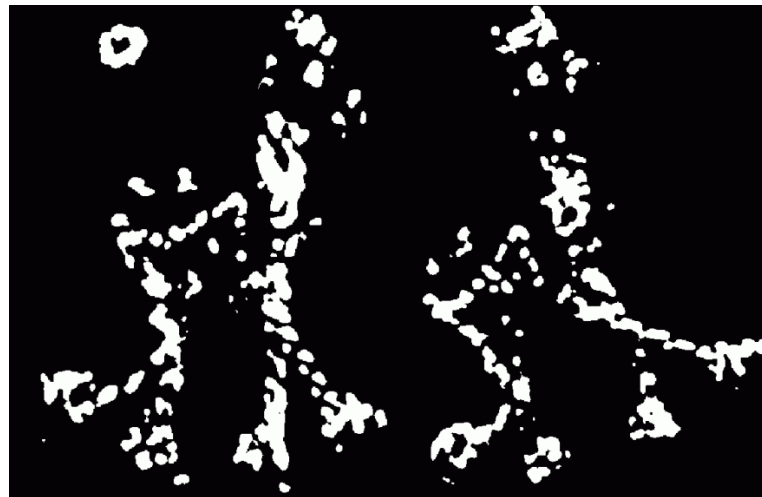
Harris Detector: Workflow

Compute corner response R



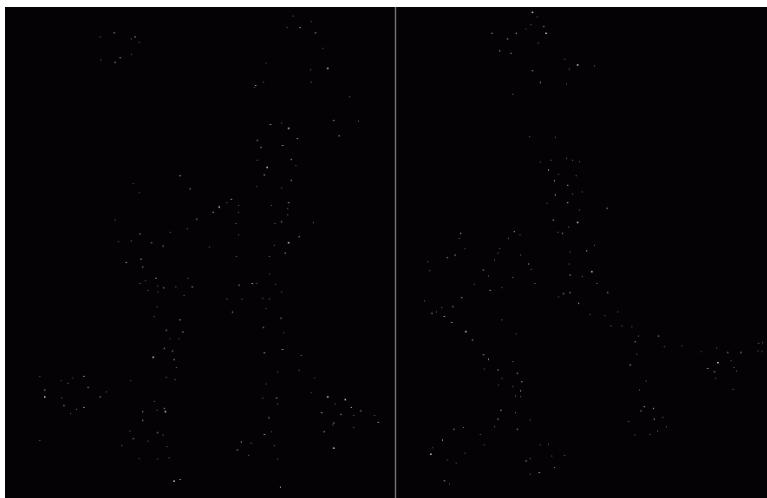
Harris Detector: Workflow

Find points with large corner response: $R > \text{threshold}$



Harris Detector: Workflow

Take only the points of local maxima of R



Harris Detector: Workflow



Harris Detector: Summary

- Average intensity change in direction $[u, v]$ can be expressed as a bilinear form:

$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

- Describe a point in terms of eigenvalues of M :
measure of corner response

$$R = \lambda_1 \lambda_2 - k (\lambda_1 + \lambda_2)^2$$

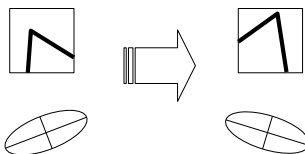
- A good (corner) point should have a *large intensity change in all directions*, i.e. R should be large positive

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Harris Detector: Some Properties

- Rotation invariance



Ellipse rotates but its shape (i.e. eigenvalues) remains the same

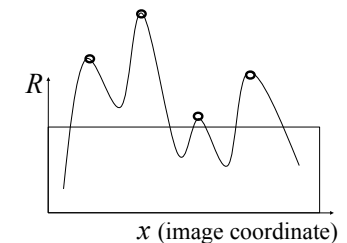
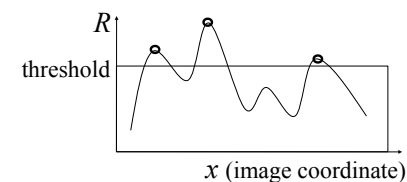
Corner response R is invariant to image rotation

Harris Detector: Some Properties

- Partial invariance to *affine intensity change*

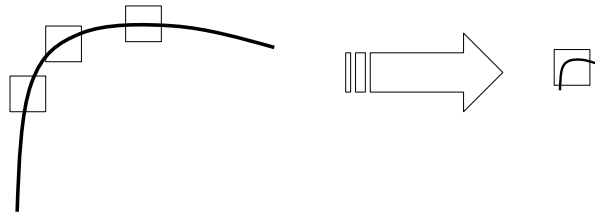
✓ Only derivatives are used \Rightarrow invariance to intensity shift $I \rightarrow I + b$

✓ Intensity scale: $I \rightarrow a I$



Harris Detector: Some Properties

- But: non-invariant to *image scale*!



All points will be
classified as edges

Corner !

ComVis1U3

ComVis1

ComVis1U3

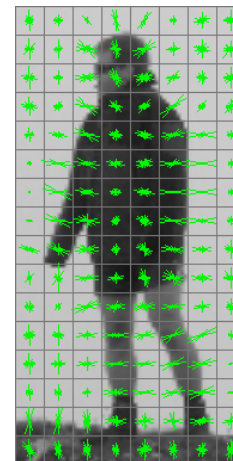
- Interest points detectors
- **Descriptors**

Image descriptors

- Descriptor: a high level representation of an image or video.
- Descriptor: a vector
- Useful for:
 - geometric based matching
 - image retrieval,
 - object recognition and categorization,
 -

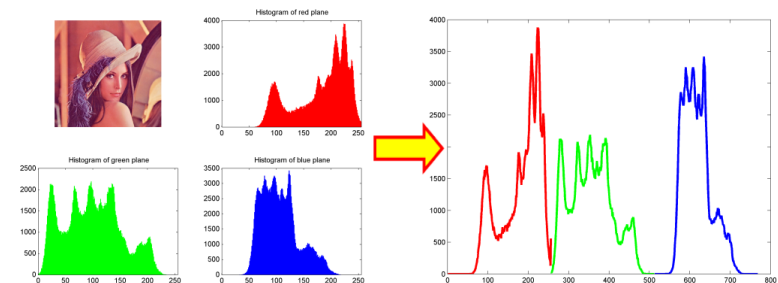
Introduction:

Dense and Sparse descriptors

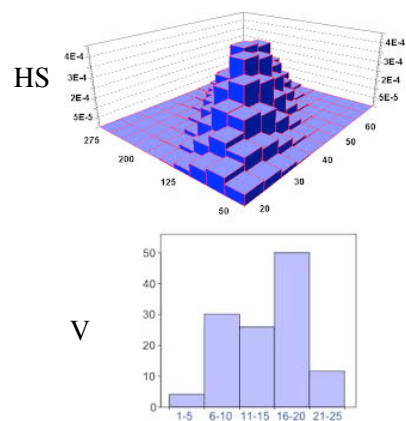
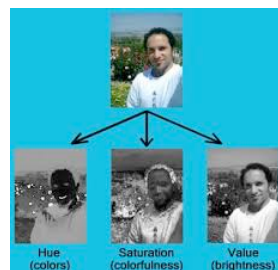


Some dense Descriptors

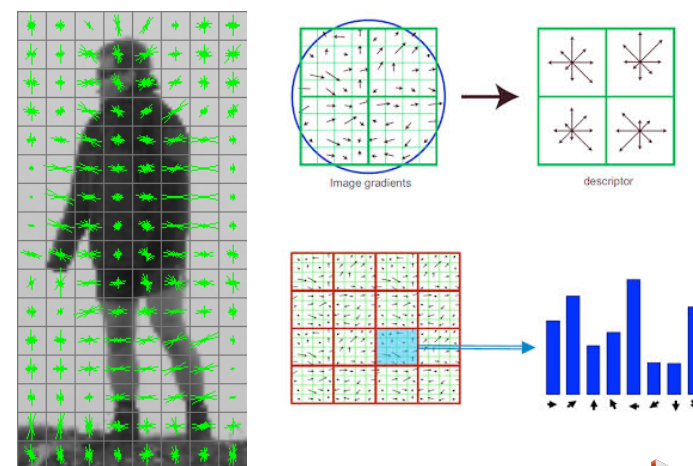
Color RGB histogram



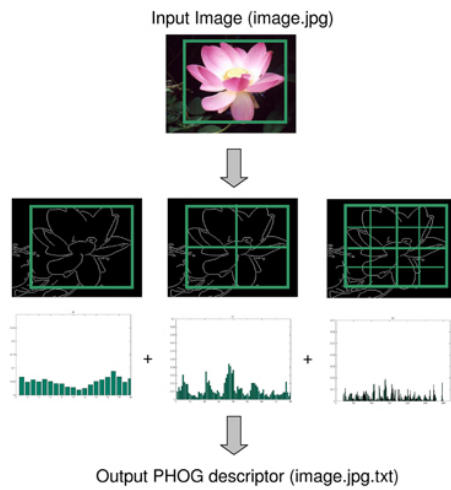
Color HS+V histogram



Histogram of oriented gradients (HOG)

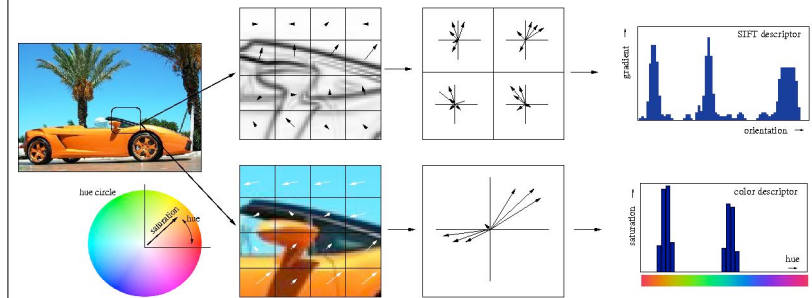


Histogram of oriented gradients (HOG)



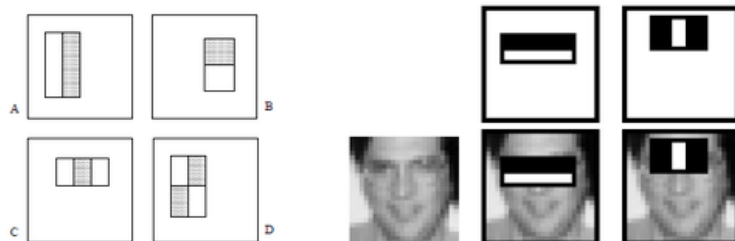
T. Chateau

Combining histograms



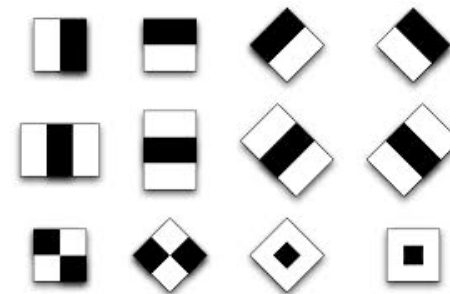
T. Chateau

Haar Wavelets



T. Chateau

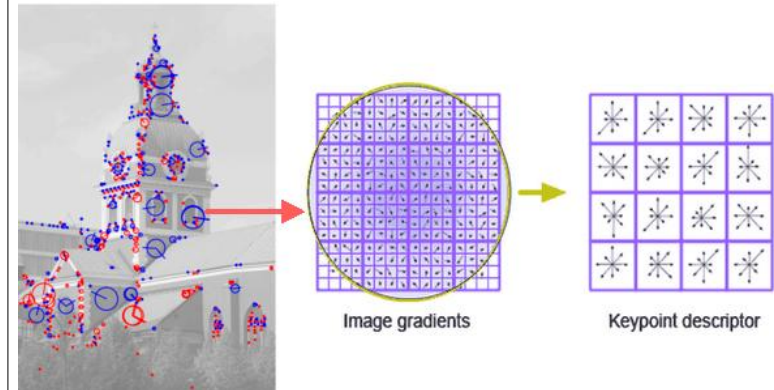
Haar Wavelets



T. Chateau

Some Sparse Descriptors

SIFT

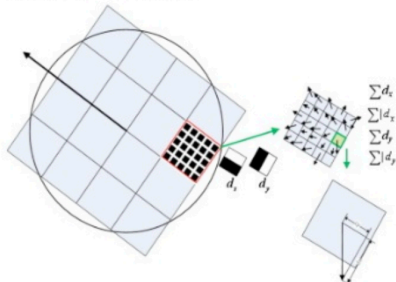


SURF

Speeded Up Robust Features **SURF**

- Approximate derivatives with Haar wavelets
- Exploit integral images

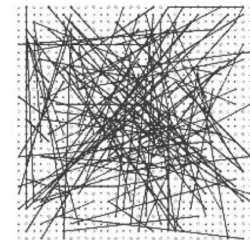
Citations:
4500 (2012)



BRIEF

Binary Robust Independent Elementary Features

- Random selection of pairs of intensity values.
- Fixed sampling pattern of 128, 256 or 512 pairs.
- Hamming distance to compare descriptors (XOR).



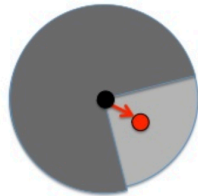
Citations:
149 (2012)

ORB

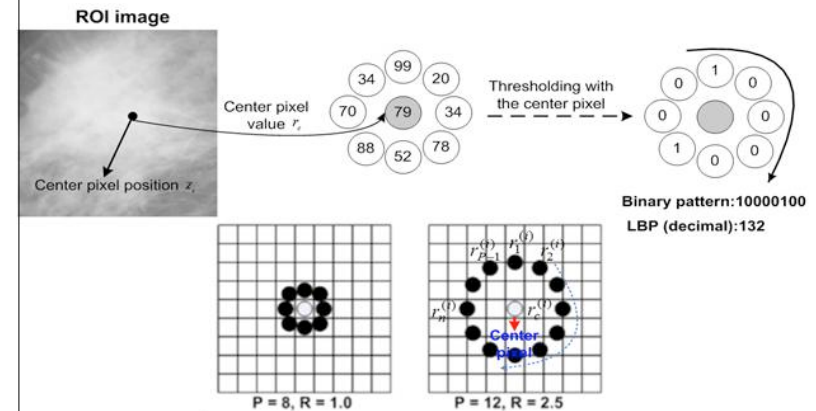
Oriented FAST and Rotated BRIEF

- Add rotation invariance to BRIEF
- Orientation assignment based on the intensity centroid

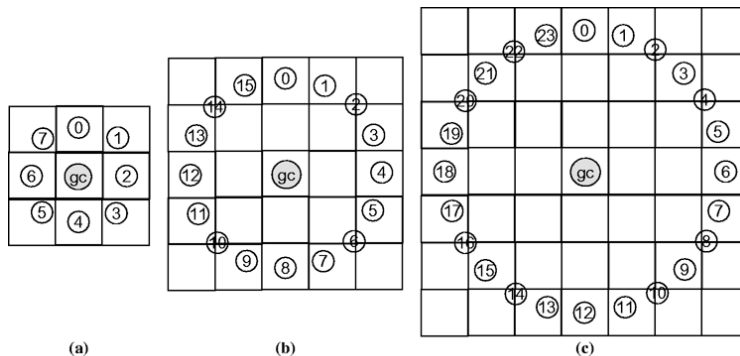
Citations:
43 (2012)



LBP: local binary pattern



LBP: local binary pattern



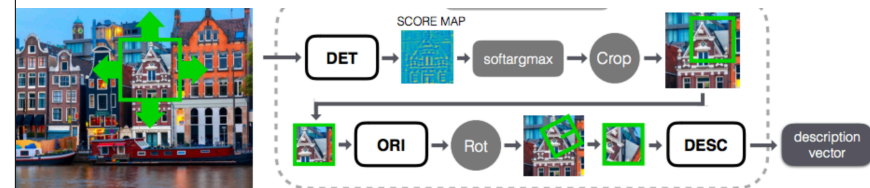
Notes: (a) $P = 8$, $R = 1$; (b) $P = 16$, $R = 2$; (c) $P = 24$, $R = 3$

LIFT: Learned Invariant Feature Transform

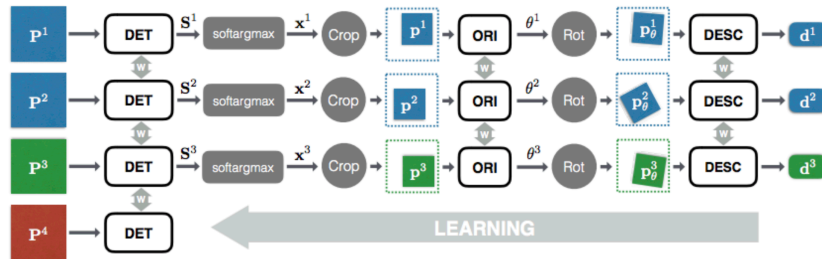
Kwang Moo Yi^{*,1}, Eduard Trulls^{*,1}, Vincent Lepetit², Pascal Fua¹

¹Computer Vision Laboratory, Ecole Polytechnique Fédérale de Lausanne (EPFL)

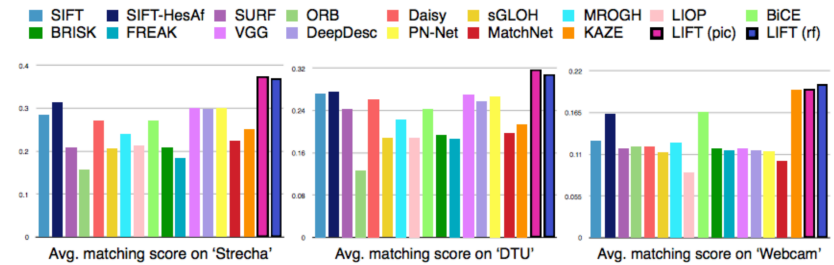
²Institute for Computer Graphics and Vision, Graz University of Technology
{kwang.yi, eduard.trulls, pascal.fua}@epfl.ch, lepetit@icg.tugraz.at



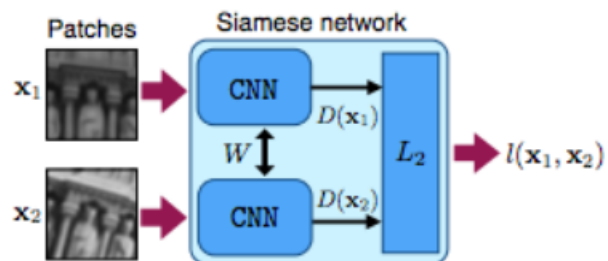
LIFT: Learned Invariant Feature Transform



LIFT: Learned Invariant Feature Transform



Deep Neural network descriptor for matching



Video based descriptors (HOG/HOF)

$$\mu = g(., \sigma_i^2; \tau_i^2) * \begin{pmatrix} L_x^2 & L_x L_y & L_x L_t \\ L_x L_y & L_y^2 & L_y L_t \\ L_x L_t & L_y L_t & L_t^2 \end{pmatrix}$$

